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CRITICALITY MEASURES FOR TIME CONSTRAINT TUNNELS IN SEMICONDUCTOR MANUFACTURING

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ABSTRACT

Semiconductor manufacturing processes include more and more (queue) time constraints often spanning multiple operations, which impact both production efficiency and quality. After recalling the problem of time constraint management, this paper focuses on the notion of criticality defined in terms of time constraints at an operational decision level. Various criticality measures are presented. A discrete-event simulation-based approach is used to evaluate the criticality of machines for time constraints. Computational experiments conducted on industrial instances are discussed. The paper ends with some conclusions and perspectives.

1 Introduction

Semiconductor manufacturing processes are known to be the most complex manufacturing processes. They are characterized by long cycle times (8 to 12 weeks) with up to one thousand operations (often called *steps*), re-entrant flows, and heterogeneous complex machines. In addition to these challenging features, the constant development of new technology nodes fosters the multiplication of so-called *Time Constraints* (TCs) i.e., time limits to be respected between two operations in a given product route (Lima et al. 2021). More broadly, *Time Constraint Tunnels* (TCTs) are defined as a set of consecutive steps under at least one TC. Exceeding TCs may affect cycle times and production yield. Within a high-mix and highly time-varying manufacturing environment, operators working in a semiconductor manufacturing facility (*fab* in short) can have trouble detecting in real time the source (e.g., tense areas to focus) and the severity (e.g., duration of TCT overrun) of the risks of exceeding a TC when sending a lot in a TCT due to its complexity and variability. To tackle this problem, a simulation-based approach has been developed and Key Performance Indicators (KPIs) suggested to help the operators focus on different parts of the fab by Sadeghi et al. (2015), Lima et al. (2021) and Anthouard et al. (2022). Among these KPIs, the present paper proposes and discusses a number of criticality measures in terms of time constraints to support the management of TCTs at an operational decision level.

In the literature, TC management is a relatively recent topic. Problems including TCs in the constraints can be classified in three categories: Scheduling, capacity planning, and production control. To the best of our knowledge, no paper discusses the notion of criticality in terms of TCs. Criticality is mainly discussed for shifting bottleneck heuristics developed to solve scheduling problems minimizing the maximum lateness (*Lmax*) (Holtsclaw and Uzsoy 1996) or the Total Weighted Tardiness (TWT) (Zimmermann and Mönch 2006). In the shifting bottleneck heuristic, machine groups are ordered to be computed according to a criticality measure (Adams et al. 1988; Dauzère-Pérès and Lasserre 1993). The criticality measure chosen influences the sequence of the scheduling sub-problems to solve, and thus the quality of the best found

solution. Different criticality measures can be found in the literature, focused mainly on the capacity of the fab and the tardiness. Holtsclaw and Uzsoy (1996) propose two criticality measures based on the workload of groups of machines and several approaches to compute *Lmax* as criticality measure. Pinedo (2012) uses a similar approach to study the TWT as a criticality measure. Zimmermann and Mönch (2006) propose a critical measure based on the previous measures and two other dynamic measures that rely on the workload of groups of machines and on a slack-based criticality measure comparing the processing time left and the due date of every lot. Aytug et al. (2003) propose static criticality measures based on the remaining processing time, the number of remaining operations, and the total machine load. Additionally, dynamic critical measures are proposed by studying the scheduling problem with an infinite capacity and looking at the violation (total, average, and maximal) of the capacity over time. For production control, Kopp et al. (2020) propose several dispatching schemes based on TC critical ratios and slack that could be adapted to create new measures.

To the best of our knowledge, criticality measures are not defined through the prism of TCs in the literature. The main difference between classical due dates and TCs is that a lot can be under multiple due dates at the same time when several TCs overlap in a single TCT, or have no due date if it is not under a TC. In addition, criticality measures are usually provided in the literature to support the search of the best machine sequence within the shifting bottleneck heuristics. This differs from our goal, which is to find the most critical machines in terms of TCs to identify the weak TC areas and avoid TCs being exceeded.

This paper presents criticality measures for time constraints. The context for our analysis does not take into account abnormal conditions (e.g., machine breakdowns or recoveries). Several measures from the existing literature are adapted in terms of TCs, and new measures are proposed. The conducted analysis shows that static measures are useful, but not sufficient to conclude on the criticality of machines. Strengthened by dynamic criticality measures, valuable support can be derived and a selection of machines proposed to the operators to focus on.

The remainder of this paper is organized as follows. Section 2 motivates and defines the problem under study. Criticality measures are detailed in Section 3. The proposed criticality measures are then evaluated and compared in Section 4 using full fab industrial instances. The interest of dynamic criticality measures is presented before concluding in Section 5.

2 TCT MANAGEMENT: PROBLEM STATEMENT AND SOLUTION APPROACH

As stated in Section 1, time constraints are hard to manage in a high-mix production environment. Because of the time-dependent character, operators need real-time indicators to know where they should concentrate their effort (lot, machine, TC). Moreover, sending a lot in a TCT is an important decision as once a lot is in the TCT, it must perform all its processing steps without being slowed down or stopped for too long to respect all the TCs. Thus, operators need to estimate the potential risks induced when sending lots in TCTs and identify the weak areas of the tunnels. This paper focuses on the definition and analysis of criticality measures in terms of TCs. The goal is to create a set of measures to characterize the criticality of the machines in a fab. Two components are required to characterize the criticality of a TC: A flag that indicates if the TC can be exceeded, and a time length measuring the time the TC has been exceeded.

Let us distinguish two evaluation modes of machine criticality in terms of TCs: (i) *Criticality under normal conditions:* Under normal conditions, the criticality of a given machine depends on the number of lots to be processed in TCs. If no action is taken, the machine will be overloaded by lots under the TCs and could lead to TCs being exceeded. Under normal conditions, all the machines in the fab stay in their original state. (ii) *Criticality under abnormal conditions:* Under abnormal conditions, the criticality of a given machine depends on its state. A downtime on the machine could lead to TCs being exceeded. Under abnormal conditions could lead to TCs being exceeded. Under abnormal conditions, the criticality of a given machine depends on its state. A downtime on the machine could lead to TCs being exceeded. Under abnormal conditions, states of machines can change (i.e., breakdown, disqualifications). By studying the criticality of the machines in a TCT, the risks of sending lots in the TCT can be reduced by focusing on the critical machines.

3 CRITICALITY MEASURES

In this section, a number of criticality measures are adapted to the problem of TCT management, and new criticality measures are also introduced. Measures are divided into two groups: (i) *Static measures:* Summary measures computed based on historical data related to the lot processing (see Section 3.1), (ii) *Dynamic measures:* Time-dependent measures computed dynamically using real-time data of the lots at their current steps (see Section 3.2). Table 1 details the notations used in the paper.

| Table | 1: | Notations. |
|-------|----|------------|
| | | |

| Notation | Description |
|---------------------|--|
| R | Set of simulation runs r |
| Н | Time horizon of the schedule |
| S_k | Set of steps s that can be processed on machine k |
| S_{cs} | Set of remaining steps \tilde{s} of TC c after step s (included) |
| S_{kr}^{c} | Set of steps s under TC c processed on machine k during run r |
| S_{crst}^{κ} | Set of remaining steps \tilde{s} of TC c after step s (included) at period t on run r |
| S_{krt}^{c} | Set of steps s under TC queuing on machine k at period t of run r |
| C_s^{n} | Set of constraints c of step s |
| C_{rs} | Set of constraints c of step s entered during run r |
| C_{rst} | Set of constraints c of step s at period t of run r |
| K_s | Set of machines k qualified to process step s |
| d_{ks} | Delay between step s and its successor on machine k |
| p_{ks} | Processing time of step s on machine k |
| T_s^{CT} | Estimated cycle time for step s including the waiting time before and the processing time of s |
| τ_{crst} | Time a given lot performing step s passed under TC c during run r at period t |
| τ_{crs} | Time a given lot that performed step s passed under TC c at the end of run r |
| T_c^{max} | Maximum baseline duration of TC c |
| Ws | Weight associated to step s |

3.1 Static Criticality Measures

Static criticality measures are usually fast to compute as they usually require no algorithm. A number of static criticality measures from the literature are adapted and presented in this section.

Static Total Tool Load (denoted by STTL), $m(STTL) \in \mathbb{R}^+$: Based on the processing times, this measure is introduced by Aytug et al. (2003) and Holtsclaw and Uzsoy (1996) to detect machines that could bottleneck the fab. Processing time is not the only factor causing bottleneck situations. With parallel multi-chamber machines, batch machines, and serial multi-chamber machines, processes can overlap. Measure STTL (i.e., time to process all the steps on a given machine) corresponds to the sum of d_{ks} , and the average of processing time p_{ks} of all the steps s in S_k processing on machine k:

$$m_k(\text{STTL}) = \sum_{s \in S_k} d_{ks} + \frac{1}{|S_k|} \times \sum_{s \in S_k} p_{ks}$$
(1)

To make measure STTL TC-aware (denoted by STTL_TC), we replace S_k by the set of processing steps under TCs in Equation (1).

Average Remaining Steps to Completion (denoted by ARSC), $m(\text{ARSC}) \in \mathbb{R}^+$: This measure is introduced by Aytug et al. (2003) and adapted for TCs. The intuition is that steps at the beginning of TCs are more critical as the lots have a lower priority. Lots could wait more in the first steps than in the last steps, and waiting in the first steps has more impact on the remainder of the routes than waiting in the last step. When TCs start to be critical (i.e., when the time left under TC is only of a few hours), the priority of the lots in the system increases automatically to speed up the lot in its last processing steps. In addition, ARSC takes into account that TCs overlapping more steps are more critical. Measure ARSC is computed as the average number of steps $|S_{cs}|$ to complete the TC of all steps processed on machine k as in Equation (2):

$$m_k(\text{ARSC}) = \frac{1}{\sum_{s \in S_k} |C_s|} \sum_{s \in S_k} \sum_{c \in C_s} |S_{cs}|$$
(2)

Average Remaining Processing Time (denoted by ARPT), $m(\text{ARPT}) \in \mathbb{R}^+$: This measure is presented by Aytug et al. (2003). The idea of ARPT, when extended to deal with TCs, is similar to ARSC, but instead of counting the steps left to complete the TC, the average processing time to complete every step until the completion of the TC is considered, as specified in Equation (3). Note that the average processing time is considered over all the machines that can perform the step.

$$m_k(\text{ARPT}) = \frac{1}{\sum_{s \in S_k} |C_s|} \sum_{s \in S_k} \sum_{c \in C_s} \sum_{\tilde{s} \in S_{cs}} \left(\frac{1}{|K_{\tilde{s}}|} \times \sum_{k \in K_{\tilde{s}}} p_{k\tilde{s}} \right)$$
(3)

Average Remaining Cycle Time (denoted by ARCT), $m(ARCT) \in \mathbb{R}^+$: The idea is the same as ARPT, but cycle time T^{CT} is used instead of the average processing time. T_s^{CT} considers both the waiting time at step *s* and its processing time, as follows in Equation (4).

$$m_k(\text{ARCT}) = \frac{1}{\sum_{s \in S_k} |C_s|} \sum_{s \in S_k} \sum_{c \in C_s} \sum_{\tilde{s} \in S_{cs}} T_{\tilde{s}}^{CT}$$
(4)

Total Weighted Tardiness (denoted by TWT), $m(TWT) \in \mathbb{R}^+$: This measure has been presented by Holtsclaw and Uzsoy (1996), Pinedo (2012) and Zimmermann and Mönch (2006). By extension to TCs, the interest of TWT is to support the detection of exceeded TCs during a given number of runs. Total weighted tardiness for machine k is computed as the average TWT on machine k on all simulation runs. TWT on a single simulation run on a machine is the sum of the exceeded time at the end of the run of all the TCs of the steps that could have been processed on machine k weighted by the number of machines that can process the step (see Equation (5)). An exceeded TC impacts all the machines that could have processed the steps in the TC.

$$m_k(\text{TWT}) = \frac{1}{|R|} \times \sum_{r \in R} \sum_{s \in S_{kr}^c} \left(\frac{1}{|K_s|} \times \sum_{c \in C_{rs}} \max\{0, \tau_{csr} - T_c^{max}\} \right)$$
(5)

3.2 Dynamic Criticality Measures

Dynamic measures are calculated by the simulation-based approach presented by Sadeghi et al. (2015), Lima et al. (2021) and Anthouard et al. (2022). These measures are tracked for each simulation run $r \in R$ at period $t \in H$, and descriptive summary statistics (e.g., average, min, max) are calculated on R.

Weighted Dynamic Tool Load Under TC (denoted by WDTL), $m(WDTL) \in \mathbb{R}^+$: Inspired from Zimmermann and Mönch (2006), this measure tracks throughout the simulation the time to process all steps queued under a TC in front of the machine. The computation of this measure is similar to STTL_TC (see Equation (6)). Note that it is weighted by the number of machines allowed to process step *s* as the queue is shared. A machine sharing its queue with other machines is less critical than a machine that does not share its queue, and a machine with a longer queue is more critical, as lots will tend to wait more before being processed and could thus exceed their TC.

$$m_{krt}(\text{WDTL}) = \sum_{s \in S_{krt}^c} \frac{d_{ks}}{|K_s|} + \frac{1}{|S_{krt}^c|} \times \sum_{s \in S_{krt}^c} \frac{p_{ks}}{|K_s|}$$
(6)

Weighted Slack (denoted by WSLACK), $m(WSLACK) \in \mathbb{R}^+$: This measure has been introduced by Zimmermann and Mönch (2006). WSLACK can be adapted for TCs, by assimilating the due date of a given lot to the minimum date to exceed any TC. The slack (i.e., the remaining waiting time allowed without exceeding the TC) of the lot waiting to process a step on a machine is computed, normalized by the number of processing steps to complete the TC, and weighted by the priority of the lot at the step (see Equation (7)).

$$m_{krt}(\text{WSLACK}) = \sum_{s \in S_{krt}} w_s \left(\max\left\{ 1, \min_{c \in C_{rst}} \left(\frac{T_c^{max} - \tau_{crst} - \sum_{\bar{s} \in S_{crst}} \left(\frac{1}{|K_{\bar{s}}|} \times \sum_{k \in K_{\bar{s}}} p_{k\bar{s}} \right)}{|S_{crst}|} \right) \right\} \right)^{-1}$$
(7)

Criticality Level (denoted by CL), $m(CL) \in \{0, 1, 2, 3\}$: This measure provides a label comparing the time to process all the lots under a TC with the time left under the TC according to a threshold, denoted by β . The average time left under a TC for lots waiting in front of the machine at every simulation run is compared with the minimal, average, and maximal time seen in all simulation runs to process all the lots under the TC on the machine (see Equation (8)). The greater $m_{kt}(CL)$, the more complicated the processing of lots under a TC without exceeding the TC should be.

$$m_{kt}(CL) = \begin{cases} 3, & \text{if } \overline{\delta_{kt}} \leq \frac{1}{\beta} \times \min_{r \in R} \{m_{krt}(WDTL)\} \\ 2, & \text{if } \frac{1}{\beta} \times \min_{r \in R} \{m_{krt}(WDTL)\} < \overline{\delta_{kt}} \leq \frac{1}{\beta \times |R|} \times \sum_{r \in R} m_{krt}(WDTL) \\ 1, & \text{if } \frac{1}{\beta \times |R|} \times \sum_{r \in R} m_{krt}(WDTL) < \overline{\delta_{kt}} \leq \frac{1}{\beta} \times \max_{r \in R} \{m_{krt}(WDTL)\} \\ 0, & \text{otherwise} \end{cases}$$
(8)

where
$$\overline{\delta_{kt}} = \frac{1}{|R|} \times \sum_{r \in R} \left(\frac{1}{|S_{krt}^c|} \times \sum_{s \in S_{krt}^c} \min_{c \in C_{rst}} \{ \max(0, T_c^{\max} - \tau_{crst}) \} \right)$$

Number of TCs Exceeded (denoted by NTCE), $m(NTCE) \in \mathbb{N}$: This measure counts the number of TCs exceeded in front of the machine at every period. Machines with more TCs exceeded are more critical.

Dynamic Weighted Tardiness (denoted by DWT), $m(DWT) \in \mathbb{R}^+$: This measure represents the dynamic version of TWT, and is linked to NTCE. At every period, the tardiness of the jobs in front of the machine is computed and weighted by the number of machines able to process the step (see Equation (9)). Unlike TWT, there is no repercussion on DWT of previous machines when a TC is exceeded on the downstream machine. The idea is to observe when and on which machine a TC will be exceeded, and estimate the length of exceeded time.

$$m_{krt}(\text{DWT}) = \sum_{s \in S_{krt}^c} \sum_{c \in C_{rst}} \left(\frac{1}{|K_s|} \times \max\{0, \tau_{crst} - T_c^{max}\} \right)$$
(9)

Weighted Inverted Critical Ratio (denoted by WICR), $m(WICR) \in [0, \gamma]$: The critical ratio is commonly used in dispatching (Rose 2002). A ratio under 1 means the lot is behind schedule, and a ratio greater than 1 means the lot is ahead of schedule. In our case, the inverse of the critical ratio is computed and weighted with the number of machines able to process the step as a lot behind schedule is more critical than a lot ahead of schedule. To bound this measure, and in the case where a TC is exceeded, WICR for the TC is bounded by a threshold, denoted by γ . Measure WICR of machine k is then the sum of the highest WICR for all TCs of all the jobs waiting on machine k at period t (see Equation (10)).

$$m_{krt}(\text{WICR}) = \sum_{s \in S_{krt}^c} \max_{c \in C_{rst}} \{\min\{\gamma, \text{WICR}_{ckrst}\}\}, \text{ where } \text{WICR}_{ckrst} = \begin{cases} \sum_{s \in S_{crst}} \left(\frac{1}{|K_s|} \times \sum_{k \in K_s} p_{sk}\right) \\ \frac{1}{|K_s| \times (T_c^{max} - \tau_{crst})}, & \text{if } T_c^{max} > \tau_{crst} \\ \gamma, & \text{otherwise} \end{cases}$$

$$(10)$$

Number of Lots Critical (denoted by NLC), $m(NLC) \in \mathbb{N}$: This measure counts the number of critical lots i.e., lots that could exceed or have already exceeded their TCs. A machine can be critical because critical lots are queuing in front of it. To estimate whether or not a lot is critical, measure WICR is used and compared with a given threshold, denoted by α . At period *t* for machine *k*, the number of critical lots is computed as in Equation (11).

$$m_{krt}(\text{NLC}) = \sum_{s \in S_{krt}^c} LC_{krst}, \text{ where } LC_{krst} = \begin{cases} 1, & \text{if } \max_{c \in C_{rst}} \left\{ \min\left\{\gamma, \text{WICR}_{ckrst}\right\} \right\} > \alpha \\ 0, & \text{otherwise} \end{cases}$$
(11)

4 NUMERICAL EXPERIMENTS

The numerical experiments have been conducted on 45 industrial instances collected from a fab of STMicroelectronics, regularly extracted from June 2021 to April 2022. In these instances, 30% of the steps are under TC with T_c^{max} ranging from 1 hour (H) to 840H with a majority of short TCs (70% of T_c^{max} are below 24H and 40% of T_c^{max} range from 8H to 16H). TCTs include up to 25 TCs over 48 steps with an average of 3 TCs over 4 steps. TCs considered in these instances are both *end-to-start* (i.e., the TC starts at the end of a process and finishes at the beginning of another process) and *start-to-end* (i.e., the TC starts at the beginning of a process and finishes at the end of another process).

The machine criticality has been evaluated by using a discrete-event simulation-based approach, that relies on disjunctive graph modeling and list scheduling, which simulates N times the behavior of the full fab using a given dispatching rule. The output results in N different possible schedules allowing the extraction of statistical features. The simulation-based approach and instances are described by Sadeghi et al. (2015), Lima et al. (2021) and Anthouard et al. (2022). The following settings have been used: (i) The machine complexity and modus operandi (parallel multi-chamber, batch, serial multi-chamber) have been explicitly modeled. (ii) A dispatching rule using an exponential distribution based on the lot priority has been applied. (iii) The regular event triggering the extraction of dynamic data has been set to 1 hour and results in an average of 10 regular points extracted every 6 minutes. (iv) 100 runs have been performed for each instance, and a stopping condition limiting the simulation time up to 72 hours has been used, sufficient for real-time decisions. Thresholds α and β have been arbitrarily set to 0.8, and γ to 2. Cycle time T_s^{CT} is computed as follows: The waiting time is obtained by a statistical calculation based on the history of waiting times observed over the past weeks (see Chapter 4 of Dequeant (2017)). If no information is available, the waiting time is calculated according to Zachka's formula as defined by Mhiri et al. (2014). The processing times are based on the machine models provided by the Industrial Engineering experts.

4.1 Static Comparison between Criticality Measures

Let us apply the average Spearman correlation to study empirically the correlation between the proposed criticality measures (see Table 2). For all machines in the considered instances, the Spearman correlation has been calculated between every two measures and averaged over the set of instances. Table 2 shows no surprising correlation, except evident correlations such as the TOTAL values with the MAX values, and DWT with NTCE or NLC. Some medium correlations are less evident like STTL_TC with WICR and WSLACK, but otherwise, most of the other correlations were expected due to either the way of computing the measure or the correlation between the data used. A surprising result is CL that does not seem correlated to other measures, maybe due to its discrete nature.

To understand if the proposed measures identify the same subset of most critical machines among all the machines in the fab, a ranking of the machines has been made for each criticality measure. The resulting ranking lists have been compared, by highlighting the elements in common. It is worthwhile to note that the criticality of machines is one of the most vulnerable aspects in the fab, the exact ranking of these critical machines being less important. Let \mathscr{S}_m^{ρ} be the set corresponding to the $\rho \mathscr{B}$ most critical machines according to measure m. The ranking provided by two measures m_1 and m_2 are compared in terms of similarity between sets \mathscr{S}_1^{\bullet} and \mathscr{S}_2^{\bullet} . The Sørensen-Dice coefficient $DSC(\mathscr{S}_1^{\bullet}, \mathscr{S}_2^{\bullet}) \in [0, 1]$ is applied to measure the similarity between two sets as follows:

$$DSC(\mathscr{S}_1^{\bullet}, \mathscr{S}_2^{\bullet}) = \frac{2 \times |S_1^{\bullet} \cap \mathscr{S}_2^{\bullet}|}{|\mathscr{S}_1^{\bullet}| + |\mathscr{S}_2^{\bullet}|}$$

The more $DSC(\mathscr{I}_1^{\bullet}, \mathscr{I}_2^{\bullet})$ is closer to 1, the more sets \mathscr{I}_1^{\bullet} and \mathscr{I}_2^{\bullet} are similar. Table 3 shows the average similarity between the sets of critical machines provided by the proposed criticality measures for $\rho = 15\%$ over the considered instances. The label DATA_RETURNED corresponds to the percentage of machines returned by the associated measure when asking the 15% most critical machines compared to the

| | STTL | STTL_TC | ARSC | ARPT | ARCT | TWT | TOTAL_WDTL | MAX_WDTL | TOTAL_WSLAC! | MAX_WSLACK | TOTAL_CL | MAX_CL | TOTAL_NTCE | MAX_NTCE | TOTAL_DWT | MAX_DWT | TOTAL_WICR | MAX_WICR | TOTAL_NLC | MAX_NLC |
|--------------|------|---------|------|------|------|-----|------------|----------|--------------|------------|----------|--------|------------|----------|-----------|---------|------------|----------|-----------|---------|
| STTL | 100 | 60 | 11 | 11 | 17 | 36 | 37 | 26 | 35 | 16 | 4 | 4 | 25 | 24 | 25 | 24 | 28 | 12 | 26 | 25 |
| STTL_TC | 60 | 100 | 45 | 55 | 51 | 70 | 84 | 76 | 70 | 55 | 25 | 24 | 45 | 45 | 44 | 44 | 64 | 52 | 49 | 48 |
| ARSC | 11 | 45 | 100 | 78 | 75 | 35 | 36 | 38 | 48 | 54 | -7 | -6 | 17 | 18 | 17 | 18 | 40 | 46 | 18 | 19 |
| ARPT | 11 | 55 | 78 | 100 | 70 | 39 | 54 | 56 | 51 | 52 | 0 | 1 | 20 | 20 | 20 | 20 | 48 | 48 | 24 | 25 |
| ARCT | 17 | 51 | 75 | 70 | 100 | 32 | 50 | 52 | 56 | 58 | -2 | -2 | 22 | 22 | 22 | 22 | 58 | 60 | 31 | 31 |
| TWT | 36 | 70 | 35 | 39 | 32 | 100 | 60 | 55 | 74 | 67 | 16 | 16 | 59 | 58 | 59 | 58 | 66 | 63 | 62 | 61 |
| TOTAL_WDTL | 37 | 84 | 36 | 54 | 50 | 60 | 100 | 95 | 68 | 54 | 42 | 41 | 47 | 46 | 46 | 45 | 74 | 64 | 55 | 54 |
| MAX_WDTL | 26 | 76 | 38 | 56 | 52 | 55 | 95 | 100 | 62 | 53 | 39 | 38 | 46 | 45 | 45 | 45 | 69 | 64 | 53 | 52 |
| IOTAL_WSLACK | 35 | 70 | 48 | 51 | 56 | 74 | 68 | 62 | 100 | 90 | 17 | 17 | 50 | 49 | 49 | 48 | 91 | 84 | 65 | 63 |
| MAX_WSLACK | 16 | 55 | 54 | 52 | 58 | 67 | 54 | 53 | 90 | 100 | 14 | 15 | 46 | 45 | 45 | 45 | 80 | 87 | 60 | 60 |
| TOTAL_CL | 4 | 25 | -7 | 0 | -2 | 16 | 42 | 39 | 17 | 14 | 100 | - 99 | 23 | 23 | 23 | 22 | 19 | 19 | 25 | 25 |
| MAX_CL | 4 | 24 | -6 | 1 | -2 | 16 | 41 | 38 | 17 | 15 | 99 | 100 | 22 | 22 | 22 | 21 | 19 | 20 | 24 | 24 |
| TOTAL_NTCE | 25 | 45 | 17 | 20 | 22 | 59 | 47 | 46 | 50 | 46 | 23 | 22 | 100 | 100 | 100 | 99 | 48 | 53 | 82 | 83 |
| MAX_NTCE | 24 | 45 | 18 | 20 | 22 | 58 | 46 | 45 | 49 | 45 | 23 | 22 | 100 | 100 | 100 | 100 | 48 | 53 | 82 | 83 |
| TOTAL_DWT | 25 | 44 | 17 | 20 | 22 | 59 | 46 | 45 | 49 | 45 | 23 | 22 | 100 | 100 | 100 | 100 | 48 | 53 | 82 | 83 |
| MAX_DWT | 24 | 44 | 18 | 20 | 22 | 58 | 45 | 45 | 48 | 45 | 22 | 21 | 99 | 100 | 100 | 100 | 47 | 53 | 82 | 83 |
| TOTAL_WICR | 28 | 64 | 40 | 48 | 58 | 66 | 74 | 69 | 91 | 80 | 19 | 19 | 48 | 48 | 48 | 47 | 100 | 92 | 65 | 64 |
| MAX_WICR | 12 | 52 | 46 | 48 | 60 | 63 | 64 | 64 | 84 | 87 | 19 | 20 | 53 | 53 | 53 | 53 | 92 | 100 | 69 | 69 |
| TOTAL_NLC | 26 | 49 | 18 | 24 | 31 | 62 | 55 | 53 | 65 | 60 | 25 | 24 | 82 | 82 | 82 | 82 | 65 | 69 | 100 | 100 |
| MAX_NLC | 25 | 48 | 19 | 25 | 31 | 61 | 54 | 52 | 63 | 60 | 25 | 24 | 83 | 83 | 83 | 83 | 64 | 69 | 100 | 100 |

Table 2: Spearman correlation (%).

list of machines. More prominent than the Spearman correlation, the conducted analysis on the similarity between ranking lists further accentuates the disparities between static and dynamic measures. Table 3 also confirms other links between measures e.g.: (i) DWT and NTCE return similar lists at more than 90%, or (ii) WICR, NLC, and WSLACK return similar lists over 70%.

To sum up, excluding obvious correlations like the cycle time with the processing time or the remaining number of steps for completion of the TC, or the TOTAL with the MAX measures, other measures do not seem to be strongly correlated and lead to different results. Static measures give different results compared to dynamic measures and are not sufficient to state on the criticality of machines. Finally, some measures identify smaller sets of machines as critical as CL, NTCE, or DWT. More investigations need to be done to understand the scope of the information provided by each measure. In this sense, the link between dynamic measures and their interactions is investigated at a deeper level and illustrated in Section 4.2.

4.2 Dynamic Comparison between Criticality Measures

As stated in Section 2, the criticality under normal conditions is linked to the load and the management rules of the fab. As presented in Section 4.1, static and dynamic measures give different results when compared in a static way. In this section, dynamic measures have been studied in a dynamic way to better understand their behavior over time and surround the scope of the support they provide.

For the criticality under normal conditions, TWT, TOTAL_NTCE, and TOTAL_DWT highlight at the end of the simulation the risk of TCs to be exceeded. Studying them in a dynamic way adds extra information on when the TC is exceeded and can help to decide when to release a lot in a TCT, or to take other actions dedicated to preventing lots from exceeding their TCs. However, other measures are also relevant as the simulation does not take into account the multi-dimensional variability of the fab. NLC gives information

| | STTL | STTL_TC | ARSC | ARPT | ARCT | TWT | TOTAL_WDTL | MAX_WDTL | TOTAL_WSLACK | MAX_WSLACK | TOTAL_CL | MAX_CL | TOTAL_NTCE | MAX_NTCE | TOTAL_DWT | MAX_DWT | TOTAL_WICR | MAX_WICR | TOTAL_NLC | MAX_NLC | DATA_RETURNED |
|---------------|------|---------|------|------|------|-----|------------|----------|--------------|------------|----------|--------|------------|----------|-----------|---------|------------|----------|-----------|---------|---------------|
| STTL | 100 | 58 | 36 | 33 | 35 | 25 | 19 | 22 | 16 | 13 | 11 | 10 | 22 | 21 | 22 | 21 | 14 | 12 | 18 | 16 | 15 |
| STTL_TC | 58 | 100 | 36 | 43 | 39 | 36 | 35 | 36 | 20 | 11 | 25 | 23 | 34 | 32 | 32 | 32 | 20 | 16 | 27 | 25 | 15 |
| ARSC | 36 | 36 | 100 | 50 | 65 | 4 | 13 | 20 | 10 | 17 | 6 | 6 | 15 | 17 | 16 | 17 | 8 | 14 | 8 | 13 | 15 |
| ARPT | 33 | 43 | 50 | 100 | 58 | 7 | 32 | 38 | 19 | 17 | 19 | 19 | 19 | 19 | 18 | 18 | 22 | 19 | 19 | 20 | 15 |
| ARCT | 35 | 39 | 65 | 58 | 100 | 6 | 25 | 31 | 21 | 25 | 11 | 11 | 20 | 20 | 19 | 20 | 20 | 23 | 19 | 22 | 15 |
| TWT | 25 | 36 | 4 | 7 | 6 | 100 | 37 | 35 | 44 | 29 | 28 | 26 | 48 | 45 | 46 | 45 | 37 | 34 | 47 | 42 | 15 |
| TOTAL_WDTL | 19 | 35 | 13 | 32 | 25 | 37 | 100 | 77 | 43 | 25 | 48 | 43 | 52 | 49 | 51 | 49 | 54 | 45 | 60 | 56 | 15 |
| MAX_WDTL | 22 | 36 | 20 | 38 | 31 | 35 | 77 | 100 | 40 | 25 | 42 | 39 | 54 | 53 | 53 | 52 | 50 | 45 | 58 | 56 | 15 |
| TOTAL_WSLACK | 16 | 20 | 10 | 19 | 21 | 44 | 43 | 40 | 100 | 69 | 37 | 35 | 47 | 44 | 43 | 42 | 73 | 65 | 67 | 61 | 15 |
| MAX_WSLACK | 13 | 11 | 17 | 17 | 25 | 29 | 25 | 25 | 69 | 100 | 27 | 28 | 36 | 35 | 33 | 33 | 53 | 60 | 50 | 50 | 15 |
| TOTAL_CL | 11 | 25 | 6 | 19 | 11 | 28 | 48 | 42 | 37 | 27 | 100 | 90 | 37 | 36 | 37 | 36 | 39 | 39 | 43 | 42 | 17 |
| MAX_CL | 10 | 23 | 6 | 19 | 11 | 26 | 43 | 39 | 35 | 28 | 90 | 100 | 35 | 35 | 35 | 34 | 36 | 37 | 39 | 40 | 18 |
| TOTAL_NTCE | 22 | 34 | 15 | 19 | 20 | 48 | 52 | 54 | 47 | 36 | 37 | 35 | 100 | 90 | 89 | 86 | 49 | 55 | 66 | 69 | 17 |
| MAX_NTCE | 21 | 32 | 17 | 19 | 20 | 45 | 49 | 53 | 44 | 35 | 36 | 35 | 90 | 100 | 91 | 91 | 47 | 56 | 63 | 69 | 17 |
| TOTAL_DWT | 22 | 32 | 16 | 18 | 19 | 46 | 51 | 53 | 43 | 33 | 37 | 35 | 89 | 91 | 100 | 94 | 48 | 56 | 63 | 68 | 17 |
| MAX_DWT | 21 | 32 | 17 | 18 | 20 | 45 | 49 | 52 | 42 | 33 | 36 | 34 | 86 | 91 | 94 | 100 | 47 | 56 | 61 | 67 | 17 |
| TOTAL_WICR | 14 | 20 | 8 | 22 | 20 | 37 | 54 | 50 | 73 | 53 | 39 | 36 | 49 | 47 | 48 | 47 | 100 | 75 | 77 | 69 | 15 |
| MAX_WICR | 12 | 16 | 14 | 19 | 23 | 34 | 45 | 45 | 65 | 60 | 39 | 37 | 55 | 56 | 56 | 56 | 75 | 100 | 73 | 76 | 15 |
| TOTAL_NLC | 18 | 27 | 8 | 19 | 19 | 47 | 60 | 58 | 67 | 50 | 43 | 39 | 66 | 63 | 63 | 61 | 77 | 73 | 100 | 84 | 15 |
| MAX_NLC | 16 | 25 | 13 | 20 | 22 | 42 | 56 | 56 | 61 | 50 | 42 | 40 | 69 | 69 | 68 | 67 | 69 | 76 | 84 | 100 | 15 |
| DATA_RETURNED | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 17 | 18 | 17 | 17 | 17 | 17 | 15 | 15 | 15 | 15 | 0 |

| Twole of funding billing of the off off off off off off of the off official indefinites (/ / / | Table 3 | 3: | Ranking | similarity | between | criticality | measures: | 15% | most critic | cal machines | (% |). |
|---|---------|----|---------|------------|---------|-------------|-----------|-----|-------------|--------------|----|----|
|---|---------|----|---------|------------|---------|-------------|-----------|-----|-------------|--------------|----|----|

of lots close to exceeding their TCs and constituting an actual risk. Measures such as WDTL, CL, NLC, or WSLACK need to be studied dynamically to understand how machines are overloaded by lots under TCs. When these measures present large values, it is a sign that it can be complicated to process lots under a TCT without exceeding their TCs. A simulation time horizon up to 72 hours could be insufficient for these measures to inform on TC violations. Sending a lot at specific time *t* in a TCT with large WDTL, CL, NLC, or WSLACK could lead to TCs being exceeded after the end of the simulation depending on when the peak of these measures is reached. A major point worth noting is that simulating a longer time horizon implies larger computational times, which can be critical for real-time decisions.

Dynamic measures have been studied in a dynamic way to evaluate their predictive capabilities related to the TC violation, in particular: (i) If whenever TCs started to be exceeded (first triggers of NTCE without breaks), is the violation detected by measures not later than 48 hours before (see Table 4)?, or (ii) When criticality measures are triggered, does this indicate that TCs will be exceeded later by the end of 48 hours (see Table 5)?. The dynamic measures have been studied (i) independently to understand the behaviors of the measures with respect to NTCE, and (ii) combined to investigate the value of their interactions. To avoid any risk of exceeding TCs, the trigger values of DWT, NTCE and CL have been defined to be strictly positive. Note that measure CL is critical when positive, by definition. For this reason, only NTCE is represented as DWT, and NTCE gives similar information. The trigger values for WDTL, WICR, NLC and WSLACK have been arbitrary defined equal to their average values for the instance and machine under study. The idea is to detect peaks in the signal sent by measures, that could be a sign of a machine being critical. Tables 4 and 5 represent the average values for all the instances. The row Trigg indicates the average percentage of times, per machine and instance, that measures are triggered.

| | t-46H,t-48H | t-43H,t-45H | t-40H,t-42H | t-37H,t-39H | t-34H,t-36H | t-31H,t-33H | t-28H,t-30H | t-25H , t-27H | t-22H,t-24H | t-19H,t-21H | t-16H,t-18H | t-13H,t-15H | t-10H,t-12H | t-7н , t-9н | t-4H,t-6H | t-1H, t-3H | t | Trigg |
|---------------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|----------------------|-------------|-------------|-------------|-------------|-------------|--------------------|-----------|------------|-----|-------|
| NTCE | 33 | 35 | 36 | 38 | 39 | 41 | 42 | 43 | 44 | 44 | 45 | 46 | 48 | 48 | 49 | 40 | 100 | 39 |
| MIN_WDTL | 53 | 50 | 48 | 48 | 46 | 46 | 44 | 44 | 44 | 43 | 44 | 43 | 43 | 44 | 44 | 43 | 39 | 29 |
| AVG_WDTL | 63 | 62 | 60 | 58 | 57 | 56 | 55 | 54 | 53 | 53 | 53 | 53 | 53 | 53 | 54 | 53 | 50 | 39 |
| MAX_WDTL | 62 | 62 | 62 | 62 | 62 | 63 | 64 | 63 | 63 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 53 | 43 |
| CL | 3 | 3 | 3 | 3 | 3 | 4 | 4 | 3 | 4 | 3 | 3 | 4 | 5 | 6 | 8 | 10 | 10 | 18 |
| WICR | 54 | 53 | 51 | 52 | 52 | 53 | 52 | 52 | 52 | 52 | 52 | 52 | 52 | 53 | 54 | 52 | 57 | 39 |
| NLC | 39 | 38 | 37 | 38 | 39 | 40 | 41 | 41 | 42 | 42 | 42 | 43 | 44 | 45 | 46 | 49 | 58 | 29 |
| WSLACK | 61 | 58 | 58 | 59 | 58 | 57 | 55 | 55 | 55 | 54 | 55 | 54 | 54 | 54 | 55 | 55 | 51 | 41 |
| MIN_WDTL & AVG_WDTL | 43 | 41 | 39 | 37 | 36 | 36 | 35 | 34 | 33 | 33 | 34 | 34 | 34 | 35 | 36 | 35 | 34 | 26 |
| MIN_WDTL & MAX_WDTL | 37 | 35 | 34 | 34 | 32 | 33 | 32 | 32 | 31 | 32 | 32 | 33 | 33 | 34 | 34 | 34 | 30 | 24 |
| MIN_WDTL & CL | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 | 1 | 2 | 3 | 4 | 5 | 5 | 9 |
| MIN_WDTL & WICR | 29 | 25 | 24 | 24 | 23 | 23 | 23 | 22 | 22 | 22 | 22 | 21 | 21 | 22 | 23 | 23 | 25 | 17 |
| MIN_WDTL & NLC | 23 | 21 | 21 | 21 | 20 | 20 | 19 | 20 | 20 | 19 | 18 | 18 | 18 | 19 | 19 | 22 | 28 | 15 |
| MIN_WDTL & WSLACK | 32 | 27 | 26 | 27 | 25 | 25 | 23 | 24 | 23 | 23 | 23 | 22 | 22 | 23 | 24 | 24 | 24 | 18 |
| AVG_WDTL & MAX_WDTL | 50 | 51 | 49 | 48 | 47 | 47 | 46 | 46 | 45 | 46 | 46 | 46 | 46 | 47 | 47 | 47 | 42 | 34 |
| AVG_WDTL & CL | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 3 | 5 | 6 | 6 | 11 |
| AVG_WDTL & WICR | 33 | 32 | 30 | 30 | 30 | 29 | 29 | 29 | 28 | 27 | 28 | 27 | 27 | 29 | 30 | 29 | 32 | 22 |
| AVG_WDTL & NLC | 26 | 25 | 24 | 24 | 23 | 23 | 23 | 24 | 23 | 23 | 23 | 22 | 23 | 24 | 25 | 28 | 35 | 19 |
| AVG_WDTL & WSLACK | 35 | 34 | 32 | 32 | 31 | 30 | 29 | 28 | 28 | 27 | 28 | 27 | 27 | 28 | 30 | 30 | 29 | 22 |
| MAX_WDTL & CL | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 2 | 2 | 3 | 3 | 4 | 5 | 6 | 6 | 12 |
| MAX_WDTL & WICR | 32 | 31 | 30 | 31 | 31 | 31 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 34 | 35 | 33 | 33 | 25 |
| MAX_WDTL & NLC | 25 | 24 | 24 | 25 | 25 | 26 | 26 | 27 | 27 | 27 | 27 | 27 | 28 | 30 | 30 | 32 | 36 | 20 |
| MAX_WDTL & WSLACK | 34 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 32 | 33 | 34 | 34 | 30 | 24 |
| CL & WICR | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 3 | 4 | 4 | 11 |
| CL & NLC | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 4 | 5 | 10 |
| CL & WSLACK | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 | 4 | 5 | 5 | 11 |
| WICR & NLC | 31 | 31 | 30 | 31 | 31 | 32 | 33 | 33 | 34 | 34 | 34 | 35 | 36 | 37 | 38 | 40 | 48 | 25 |
| WICR & WSLACK | 45 | 42 | 41 | 42 | 42 | 41 | 40 | 40 | 39 | 40 | 40 | 40 | 40 | 40 | 42 | 41 | 42 | 31 |
| NLC & WSLACK | 29 | 28 | 27 | 28 | 27 | 27 | 27 | 28 | 28 | 28 | 28 | 28 | 30 | 30 | 31 | 33 | 39 | 22 |
| VALID_DATA | 27 | 30 | 34 | 37 | 40 | 43 | 47 | 50 | 53 | 58 | 62 | 67 | 72 | 78 | 84 | 88 | 100 | 0 |

Table 4: Percentage of criticality measures detecting an NTCE event before it happens (%).

The Trigg values in Table 4 and 5 can be different, as Table 4 explores the data from the machines triggered by NTCE, whereas in Table 5 every column examines the data of the machines triggered by the criticality measure in the respective column. In other words, in Table 5, the Trigg value represents the average percentage of times, per machine and instance, whose measures are triggered by a machine. The column VALID_DATA in Table 4 represents the percentage of data retrieved for every NTCE event. As the simulation runs for 72 hours, it was only possible to obtain a full 48 hours of historical data from the simulation 27% of the time, which means that an NTCE event occurred within the first 48 hours of the simulation 73% of the time.

Consider Tables 4 and 5. The first finding extracted from Table 5 is that whenever an NTCE event is triggered, it tends to stay triggered for the next 48 hours in 58% of the cases. Second, even if CL is weak, compared to the other measures when detecting NTCE events in Table 4, its triggering is more likely to predict a violation of the TC in the future more clearly than other measures. The CL detection seems to increase to 37% between 6 to 15 hours after the measure has been triggered while the NTCE detection

| | Ļ | t+1H,t+3H | t+4H , t+6H | t+7H , t+9Н | t+10H,t+12H | t+13H , t+15H | t+16H,t+18H | t+19H , t+21H | t+22H , t+24н | t+25H , t+27H | t+28H , t+30H | t+31H , t+33H | t+34H , t+36H | t+37H , t+39H | t+40H , t+42H | t+43H , t+45H | t+46H , t+48H | Trigg |
|---------------------|-----|-----------|--------------------|--------------------|-------------|----------------------|-------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|-------|
| NTCE | 100 | 96 | 90 | 86 | 83 | 80 | 77 | 75 | 73 | 71 | 69 | 68 | 66 | 64 | 62 | 60 | 58 | 39 |
| MIN_WDTL | 29 | 33 | 33 | 33 | 33 | 32 | 30 | 29 | 27 | 26 | 24 | 23 | 21 | 20 | 19 | 18 | 18 | 20 |
| AVG_WDTL | 18 | 20 | 20 | 20 | 20 | 19 | 19 | 18 | 17 | 16 | 15 | 14 | 14 | 13 | 13 | 12 | 12 | 34 |
| MAX_WDTL | 17 | 18 | 19 | 18 | 18 | 18 | 17 | 16 | 16 | 15 | 14 | 13 | 13 | 12 | 11 | 11 | 11 | 41 |
| CL | 35 | 36 | 37 | 37 | 37 | 37 | 36 | 36 | 35 | 35 | 34 | 33 | 33 | 32 | 31 | 31 | 30 | 51 |
| WICR | 19 | 20 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 12 | 11 | 10 | 10 | 9 | 9 | 41 |
| NLC | 62 | 64 | 62 | 59 | 56 | 53 | 50 | 47 | 44 | 41 | 39 | 36 | 34 | 32 | 30 | 28 | 27 | 28 |
| WSLACK | 20 | 22 | 22 | 22 | 21 | 20 | 19 | 18 | 17 | 17 | 16 | 15 | 14 | 14 | 13 | 12 | 12 | 36 |
| MIN_WDTL & AVG_WDTL | 32 | 35 | 35 | 35 | 34 | 33 | 32 | 30 | 28 | 26 | 24 | 22 | 21 | 19 | 18 | 17 | 17 | 17 |
| MIN_WDTL & MAX_WDTL | 34 | 37 | 38 | 37 | 36 | 35 | 33 | 31 | 29 | 27 | 24 | 22 | 21 | 19 | 18 | 17 | 16 | 16 |
| MIN_WDTL & CL | 55 | 56 | 57 | 57 | 56 | 55 | 53 | 51 | 49 | 47 | 44 | 42 | 39 | 37 | 35 | 33 | 31 | 23 |
| MIN_WDTL & WICR | 39 | 41 | 41 | 40 | 37 | 35 | 32 | 30 | 27 | 24 | 21 | 19 | 17 | 15 | 14 | 13 | 12 | 11 |
| MIN_WDTL & NLC | 72 | 75 | 73 | 70 | 67 | 63 | 59 | 55 | 52 | 48 | 44 | 41 | 38 | 35 | 33 | 31 | 30 | 14 |
| MIN_WDTL & WSLACK | 41 | 44 | 44 | 44 | 42 | 39 | 37 | 34 | 31 | 28 | 26 | 24 | 21 | 20 | 18 | 17 | 16 | 11 |
| AVG_WDTL & MAX_WDTL | 20 | 22 | 22 | 22 | 21 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 12 | 11 | 28 |
| AVG_WDTL & CL | 41 | 42 | 43 | 42 | 42 | 40 | 39 | 37 | 35 | 33 | 31 | 29 | 27 | 25 | 23 | 22 | 21 | 28 |
| AVG_WDTL & WICR | 23 | 24 | 23 | 22 | 21 | 20 | 18 | 17 | 15 | 14 | 12 | 11 | 10 | 9 | 8 | 8 | 7 | 21 |
| AVG_WDTL & NLC | 64 | 67 | 65 | 62 | 58 | 55 | 51 | 48 | 45 | 41 | 38 | 35 | 32 | 30 | 28 | 26 | 25 | 18 |
| AVG_WDTL & WSLACK | 26 | 27 | 27 | 27 | 25 | 24 | 22 | 21 | 19 | 17 | 16 | 15 | 13 | 12 | 11 | 11 | 10 | 18 |
| MAX_WDTL & CL | 37 | 38 | 39 | 38 | 37 | 36 | 35 | 34 | 32 | 31 | 29 | 27 | 25 | 23 | 21 | 20 | 19 | 33 |
| MAX_WDTL & WICR | 20 | 21 | 21 | 20 | 19 | 18 | 16 | 15 | 14 | 12 | 11 | 10 | 9 | 8 | 7 | 7 | 6 | 26 |
| MAX_WDTL & NLC | 64 | 67 | 64 | 61 | 58 | 54 | 51 | 47 | 44 | 41 | 37 | 34 | 31 | 29 | 27 | 25 | 24 | 20 |
| MAX_WDTL & WSLACK | 23 | 24 | 24 | 23 | 22 | 21 | 20 | 18 | 17 | 16 | 14 | 13 | 12 | 11 | 10 | 9 | 9 | 22 |
| CL & WICR | 70 | 71 | 71 | 70 | 69 | 67 | 65 | 63 | 60 | 57 | 54 | 51 | 48 | 45 | 42 | 40 | 38 | 21 |
| CL & NLC | 83 | 84 | 84 | 83 | 82 | 80 | 77 | 75 | 72 | 68 | 65 | 61 | 58 | 54 | 51 | 49 | 47 | 28 |
| CL & WSLACK | 74 | 75 | 76 | 75 | 73 | 72 | 70 | 67 | 65 | 62 | 59 | 56 | 54 | 51 | 48 | 45 | 42 | 21 |
| WICR & NLC | 64 | 66 | 63 | 60 | 57 | 53 | 50 | 46 | 43 | 40 | 37 | 34 | 31 | 29 | 27 | 25 | 24 | 24 |
| WICR & WSLACK | 22 | 24 | 23 | 22 | 21 | 20 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 10 | 9 | 29 |
| NLC & WSLACK | 65 | 68 | 65 | 62 | 59 | 55 | 52 | 48 | 45 | 42 | 39 | 36 | 33 | 30 | 28 | 27 | 25 | 21 |

Table 5: Percentage of criticality measures predicting a NTCE event after being triggered (%).

decreases in the same period range. This is consistent with the definition of this measure, which aims to detect when a machine is overloaded by lots under TC that will exceed their TC later. NLC is efficient (i) in detecting NTCE events when they occur then (ii) in predicting if there will be TCs exceeded, once triggered. As for measure CL, NLC seems to be able to predict TCs being exceeded in the 1 to 6 hours following an NTCE trigger. This is accurate with its definition of detecting lots in advance that have not exceeded their TCs, but are likely to exceed them in the near future. Other criticality measures present many false positive alarms. Table 4 shows rather promising results in detecting NTCE triggers, but when looking at Table 5, it appears that these measures are often triggered without TCs being exceeded. In addition, as the Trigg value is the same in Tables 4 and 5 for these measures, whether a TC is exceeded or the measure triggered, they seem to be triggered for the same length of time and do not add additional information about a TC being exceeded.

As expected, when measures are considered together and both triggered at the same time (see Table 5), the quality of prediction of having TC being exceeded is increased. The best results are provided by couple (CL, NLC), which predicts with an accuracy over 80% of the time that NTCE will be triggered for the next

0 to 15 hours following a trigger of both CL and NLC. However, regarding Table 4, couple (CL, NLC) will only detect 5% of the TC being exceeded. Other associations like WICR and NLC seem to emerge with better results in detecting and predicting NTCE. More work is needed to find the best set of measures.

5 CONCLUSIONS AND PERSPECTIVES

This paper focuses on the evaluation and detection of the machine criticality in the framework of TCT management. To detect critical machines, several criticality measures, static and dynamic, have been adapted from the literature to suit the problem under study, and new criticality measures proposed. These measures have been compared based on industrial data using a simulation-based approach. The findings provided by static and dynamic measures do not always converge. Studying only the static measures is not thus sufficient to conclusively state the criticality of a machine.

Studying the criticality under normal conditions, it appears that measures TWT, NTCE, and DWT are sufficient to estimate if TCs are going to be exceeded in the time range of the simulation. More specifically, measures NTCE and DWT indicate on which machines TCs are being exceeded, while TWT completes the information with machines more likely to be at the origin of TCs being exceeded. However, as the simulation cannot be run forever, other measures have their importance when making a decision. It appears that having measures NLC and CL triggered is likely to lead to a violation of TC in the following hours. Having these measures triggered could also be a sign that more attention needs to be paid to the specific machines at the time they are triggered.

As a perspective, there is always place for improvements for the comparisons of the criticality measures. Some results have been shown in this paper but further research could be done, such as finding the best combination of measures to describe the criticality of the machines or the best detection limit, e.g., by using decision trees. In addition, for the case of the criticality under abnormal conditions, the use of capacity planning machines and scenarios could help in understanding the impact of abnormal conditions on machines and TCTs, adding new perspectives and focus points. Our ultimate goal is to propose and validate in the near future with operators at STMicroelectronics a decision support system that embeds the simulation-based approach presented and other KPIs including the estimation of criticality in terms of TCs.

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